

The Fundamental Concepts and Principles of Mechanics

2.1.1 The Fundamental Concepts

The four fundamental concepts used in mechanics are **space**, **time**, **mass** and **force**¹. It is not easy to define what these concepts are. Rather, one “knows” what they are, and they take on precise meaning when they appear in the principles and equations of mechanics discussed further below.

The concept of space is associated with the idea of the position of a point, which is described using coordinates (x, y, z) relative to an origin o as illustrated in Fig. 2.1.1.

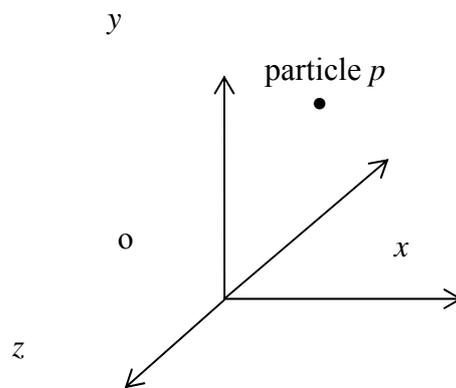


Figure 2.1.1: a particle in space

The time at which events occur must be recorded if a material is in motion. The concept of mass enters Newton’s laws (see below) and in that way is used to characterize the relationship between the acceleration of a body and the forces acting on that body. Finally, a force is something that causes matter to accelerate; it represents the action of one body on another.

2.1.2 The Fundamental Principles

The fundamental laws of mechanics are Newton’s three laws of motion. These are:

Newton’s First Law:

if the resultant force acting on a particle is zero, the particle remains at rest (if originally at rest) or will move with constant speed in a straight line (if originally in motion)

By **resultant force**, one means the sum of the individual forces which act; the resultant is obtained by drawing the individual forces end-to-end, in what is known as the **vector**

¹ or at least the only ones needed outside more “advanced topics”

polygon law; this is illustrated in Fig. 2.1.2, in which three forces \mathbf{F}_1 , \mathbf{F}_2 , \mathbf{F}_3 act on a single particle, leading to a non-zero resultant force² \mathbf{F} .

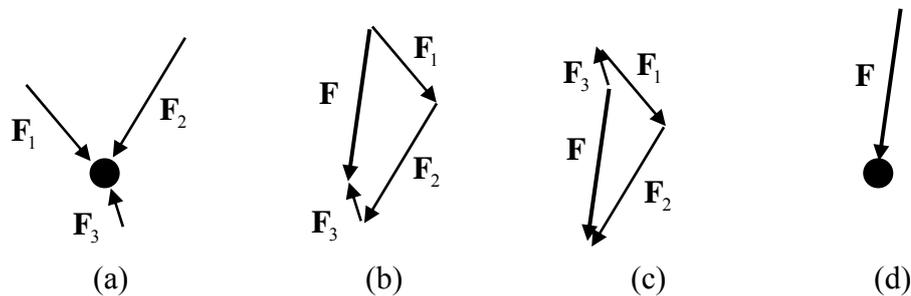


Figure 2.1.2: the resultant of a system of forces acting on a particle; (a) three forces acting on a particle, (b) construction of the resultant \mathbf{F} , (c) an alternative construction, showing that the order in which the forces are drawn is immaterial, (d) the resultant force acting on the particle

Example (illustrating Newton's First Law)

In Fig. 2.1.3 is shown a floating boat. It can be assumed that there are two forces acting on the boat. The first is the boat's **weight** \mathbf{F}_g , that is its mass times the acceleration due to gravity g . There is also an upward buoyancy force \mathbf{F}_b exerted by the water on the boat. Assuming the boat is not moving up or down, these two forces must be equal and opposite, so that their resultant is zero.

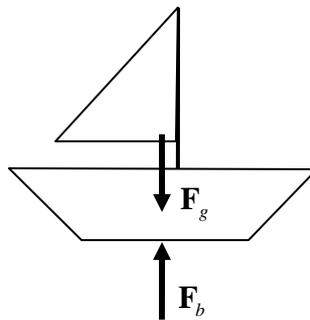


Figure 2.1.3: a zero resultant force acting on a boat

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The resultant force acting on the particle of Fig. 2.1.2 is non-zero, and in that case one applies Newton's second law:

² the construction of the resultant force can be regarded also as a principle of mechanics, in that it is not proved or derived, but is taken as "given" and is borne out by experiment

Newton's Second Law:

if the resultant force acting on a particle is not zero, the particle will have an acceleration proportional to the magnitude of the resultant force and in the direction of this resultant force:

$$\mathbf{F} = m\mathbf{a} \quad (2.1.1)$$

where³ \mathbf{F} is the resultant force, \mathbf{a} is the acceleration and m is the mass of the particle. The units of the force are the Newton (N), the units of acceleration are metres per second squared (m/s^2), and those of mass are the kilogram (kg); a force of 1 N gives a mass of 1 kg an acceleration of 1 m/s^2 .

If the water were removed from beneath the boat of Fig. 2.1.3, a non-zero resultant force would act, and the boat would accelerate at $g \text{ m/s}^2$ in the direction of \mathbf{F}_g .

Newton's Third Law:

each force (of "action") has an equal and opposite force (of "reaction")

Again, considering the boat of Fig. 2.1.3, the water exerts an upward buoyancy force *on* the boat, and the boat exerts an equal and opposite force *on* the water. This is illustrated in Fig. 2.1.4.

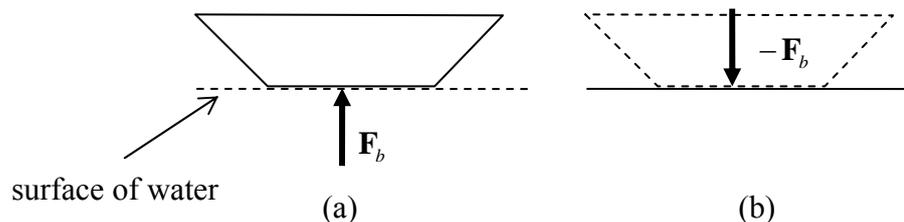


Figure 2.1.4: Newton's third law; (a) the water exerts a force on the boat, (b) the boat exerts an equal and opposite force on the water

Newton's laws are used in the analysis of the most basic problems and in the analysis of the most advanced, complex, problems. They appear in many guises and sometimes they appear hidden, but they are always there in a Solid Mechanics problem.

Source: http://homepages.engineering.auckland.ac.nz/~pkel015/SolidMechanicsBooks/Part_I/BookSM_Part_I/02_Statics_of_Rigid_Bodies/02_Statics_of_Rigid_Bodies_01_Concepts.pdf

³ **vector** quantities, that is, quantities which have both a magnitude and a direction associated with them, are represented by bold letters, like \mathbf{F} here; scalars are represented by italics, like m here. The magnitude and direction of vectors are illustrated using arrows as in Fig. 2.1.2