Abstract—Heavy metals have bad effects on environment and soils and it can uptake by natural HAP. Natural HAP is an inexpensive material that uptake large amounts of various heavy metals like Zn (II). Natural HAP (N-HAP), extracted from bovine cortical bone ash, is a good choice for substitution of commercial HAP. Several experiments were done to investigate the sorption capacity of Zn (II) to N-HAP in various particles sizes, temperatures, initial concentrations, pH and reaction times. In this study, the sorption of Zinc ions from a Zn solution onto HAP particles with sizes of 1537.6 nm and 47.6 nm at three initial pH values of 4.50, 6.00 and 7.50 was studied. The results showed that better performance was obtained through a 47.6 nm particle size and higher pH values. The experimental data were analyzed using Langmuir, Freundlich, and Arrhenius equations for equilibrium, kinetic and thermodynamic studies. The analysis showed a maximum adsorption capacity of N-HAP as being 1.562 mmol/g at a pH of 7.5 and small particle size. Kinetically, the prepared N-HAP is a feasible sorbent that retains Zn (II) ions through a favorable and spontaneous sorption process.

Keywords—Natural Hydroxyapatite, Heavy metal ions, Adsorption, Zn removal, kinetic model, bone ash

I. INTRODUCTION

Heavy metal ions flow into water from industrial activities such as electroplating industries, electronic equipment manufacturing, mining, and chemical processing plants. In addition, due to their non-biodegradability and toxic nature, they should be treated entering wastewater or better yet, separated from wastewater. Organic pollutants and heavy metals limit agricultural application of sewage sludge, however, as they tend to accumulate along the food chain and bring potential risks to animals and humans [1]. The recommendation of the World Health Organization for the safe amount of Zn (II) is 5 mg/L in drinking water [2]. The metal has also been reported to bio-accumulate into fauna and flora, creating serious ecological problems at higher concentrations.

There are various methods for the removal of heavy metals such as chemical precipitation, reverse osmosis, ion exchange, coagulation, and adsorption [2]. From these methods, adsorption is the most common due to its high uptake and the lower cost. At present, there is growing interest in using low cost, non-conventional alternative materials which are considered to be waste such as grape stalks, crop millinwaste, and sawdust, instead of traditional adsorbent for heavy metals removal from wastewater [3]. Natural Hydroxyapatite obtained from bovine cortical bone ash is a stable and inexpensive material that can be produced through a simple method. Hydroxyapatite has a good ability to remove inorganic cations, which has led to the development of its use in removing heavy metals from contaminated water [4]. Hydroxyapatite [Ca10(PO4)6(OH)2] is a unique inorganic compound because of its high removal capacity for divalent heavy metal ions, and synthetic HA has been used to remove heavy metals such as Pb, Zn, Cu, Cd, Co, and Sb from water [5], [6], [7] and [8]. The possible reaction mechanisms for metal immobilization include: (a) ion exchange processes [8], [9] and [10]; (b) surface complexation [11], [12]; (c) dissolution of HA and precipitation of new metal phosphates [13] and [14], and (d) substitution of Ca in HA by other metals during re-crystallization (co-precipitation) [9] and [15]. However, because of the limited knowledge regarding the relative contribution of each process in removing metals, it seems that the above four mechanisms could all be involved [9]. Wastewater from surface finishing and the plating industry usually contain metal-ion concentrations much higher than permissible levels. Due to their high toxicity, industrial wastewaters containing heavy metals are strictly regulated and must be treated before being discharged into the environment. Various techniques have been employed for the treatment of heavy metals including precipitation, adsorption, ion-exchange and reverse osmosis, which are usually expensive techniques. In the present research, we attempted to remove Zn (II) ions from wastewater by using natural hydroxyapatite particles obtained from bone ash. This technique is surely more economical than the above mentioned techniques. This paper works on the amount of Zn ions that uptake by natural HAP particles in different sizes by Langmuir and Freundlich isotherm equations for equilibrium, and investigates the kinetic and thermodynamic by the pseudo first and second
order models and Arrhenius equations in this sorption process.

II. MATERIALS AND METHODS

A. Materials and instruments

Bovine femur, tibia, humerus and ulna were chosen as the main starting biological material. Spongy bones were discarded and the cortical bone de-fleshed. The bone marrow and all pieces of meat and fat were removed. By using a gas torch and applying direct flame to the cleaned bone, the organic components were burned. The product of this thermal process contained some char due to the burning of the organic components. To remove the remaining char, the black powder (bone ash) was placed in an air furnace at different temperatures between 600 °C to 1100 °C for 3 hours, and then was finally left to cool inside the furnace. Following this process, the black ash turned into a white granular powder[16].

All the materials and aqueous solutions were prepared using double distilled water and the Zn solution was prepared from Zn(NO3)2·6H2O diluted in deionized water. A Multiline 330i pH-meter was used to determine pH. Various buffer solutions of different pH values (4.50, 6.00, and 7.50) were used in these experiments. 0.1 M HCl and 0.1 M NaOH solutions were used to adjust the initial pH of the solution. To determine the amount of Zn in the solution, an AA-680 atomic absorption /flame emission spectrophotometer made by Shimadzu Company was used.

B. Sorption Experiments

To determine the amount of Zn (II) sorbed on N-HAP the following equation can be used:

\[ q_e = \frac{(C_0 - C_e) \times V}{m} \]  

Where \( C_0 \) is the initial concentration of metal ion (mmol/L) and \( C_e \) is the concentration of metal ions after equilibrium. \( V \) and \( m \) are volume solution (L) and mass of adsorbent (g), respectively, whereas \( q_e \) is the adsorption capacity per unit mass of N-HAP (mmol/g);

1. Equilibrium Isotherm

There are several models that express a relation between the amounts of sorption and the residual solute concentration. The most frequent models are the Langmuir and Freundlich adsorption isotherm models:

Langmuir is the most important model of monolayer adsorption, based on the assumption that there are a fixed number of adsorption sites, and each site can hold only one adsorbate molecule (the adsorbed layer is one molecule in thickness). All sites are equivalent and there is no interaction between the adsorbed molecules [3].

0.2 g of N-HAP was added to 200mL of Zn solution with three different pH values and was then poured in to a flask and placed in a shaking incubator at a speed of 300 rpm to measure the adsorption of N-HAP in various times of 5, 10, 15, 30, 60, 120, 240, 480,720 and 960 minutes.

The distribution ratio (\( K_d \)) and removal efficiency (E) of the adsorbent on the Zn (II) ions were measured as follows:

\[ K_d = \frac{\text{amount of Zn in adsorbent}}{\text{amount of Zn in solution}} \times \frac{v}{m} \]  

\[ E(\%) = \frac{C_0 - C_e}{C_0} \times 100 \]

Where \( C_0 \) and \( C_e \) are the initial and final equilibrium concentrations (mmol/g), \( v \) is the volume of the solution (mL) and \( m \) is the weight of the adsorbent (g). This equation can be expressed as follows:

\[ \text{removal efficiency (\%)} = \frac{100K_d}{K_d + \frac{v}{m}} \]  

The Freundlich isotherm model is an experimental model, usually expressed by the following equation:

\[ q_e = K_Fc_e^{1/n} \]  

Or can be expressed in a logarithmic form as:

\[ \ln q_e = \ln K_F + \frac{1}{n} \ln c_e \]

Where \( K_F \) is the Freundlich constant and \( b \) is the Freundlich exponent.
the experimental data. The study of sorption kinetics describes the solute uptake rate and evidently this rate controls the residence time of adsorbate uptake at the solid/solution interface \[17\]. In this paper, the research is on reaction based models that contain pseudo first and second order models.

To investigate the reaction-based model, pseudo-first-order and pseudo-second-order models were employed. The pseudo-first-order model and pseudo-second-order model can be expressed by Eqs. (8) and (9), respectively:

\[
\frac{dq}{dt} = k_1(q_e - q_t) \tag{9}
\]

\[
\frac{dq^2}{dt^2} = k_2(q_e - qt)^2 \tag{10}
\]

Solving equation 9 and 10 for the initial and boundary conditions of \(t=0\) to \(t=t\) and \(q_t=0\) to \(q_t=q_0\), the following equations can be obtained:

\[
\log(q_e - q_t) = \log q_e - \left(\frac{k_1}{2.303}\right)t
\]

\[
\frac{t}{q_t} = \frac{1}{k_2q_e^2} + \frac{t}{q_e} \tag{11}
\]

3. Adsorption Thermodynamic Studies

Standard enthalpy change (\(\Delta H^\circ\)), standard free energy change (\(\Delta G^\circ\)) and standard entropy change (\(\Delta S^\circ\)) are thermodynamic parameters that can be obtained by the following equations:

\[
K_e = \frac{q_e}{c_e} \tag{13}
\]

\[
\Delta G^\circ = -RT \ln K_e \tag{14}
\]

\[
\ln K_e = \frac{-\Delta H^\circ}{R} + \frac{\Delta S^\circ}{R} \tag{15}
\]

Thermodynamic experiments were carried out at a temperature range of 15°C to 55°C and in these equations, the temperature unit is (K).

Another important equation in thermodynamic investigations is the Arrhenius equation. A modified Arrhenius-type equation related to the surface coverage (\(\theta\)) is sticking probability, \(S^*\). This is a function of the adsorbate/adsorbent system, which is a measure of the potential of an adsorbate to remain on the adsorbent indefinitely. The Arrhenius equation can be expressed as \[18\]:

\[
S^* = (1 - \theta)\exp\left(-\frac{E_a}{RT}\right) \tag{16}
\]

Where \(\theta\) is surface coverage:

\[
\theta = 1 - \frac{C_e}{C_0} \tag{17}
\]

Where \(E_a\) is activation energy and \(R\) is the universal gas constant (8.314 J mol\(^{-1}\) K\(^{-1}\)).

III. RESULTS AND DISCUSSION

A. Equilibrium Studies

Values of \(q_{\text{max}}\) and \(b\) were determined from the linear plot of \(C_e/\theta\) versus \(C_e\) that were listed with the correlation coefficients (\(R^2\)) in Table 2, and with the linear plot of \(\ln q_e\) versus \(\ln C_e\). By using Freundlich isotherm model, the values of \(bF\) and \(KF\) were obtained and shown in Table III. In the initial concentrations of the Zn ion solution that was between 0.1 to 1.2 mmol/L, the sorption data showed a good fit with the Freundlich isotherm model and it had a better fit than the Langmuir isotherm model (\(R^2 = 0.99\)). Figures 1 and 2 were plotted for the Langmuir isotherm model and Figs. 3 and 4 were for the Freundlich isotherm model for sorption of Zn (II) ions on N-HAP in different particle sizes and pH values. The maximum capacity of sorption (\(q_{\text{mon}}\)) and the constant for the two models that were listed in Table 2 showed better sorption for Zn (II) ions in higher pH values and the 47.6 nm size. The maximum capacity of sorption was 1.562 mmol/g for pH=7.50. Application of the Freundlich model to the equilibrium data of Zn(II) ion indicates the monolayer coverage of N-HAP by the Zn(II) ion, but this was to non-distinct or multiple sites of adsorption, unlike the Langmuir model, which is to distinct localized adsorption sites.

Table IV shows the values of \(R_L\) for the initial concentration of 0.1 mmol/L and different pH values that show favorable isotherm sorption with respect to Table I and the following table.

![Fig. 1 Langmuir isotherm model for 47.6 nm size natural HAP particles](image1)

![Fig. 2 Langmuir isotherm model for 1537.6 nm size natural HAP particles](image2)

![Fig. 3 Freundlich isotherm model for 47.6 nm size natural HAP particles](image3)
Fig. 4 Freundlich isotherm model for 1537.6 nm size natural HAP particles

Fig. 5 Removal efficiency of N-HAP

Fig. 6 Pseudo-first order rate constants for adsorption of the zinc ion onto natural HAP

Fig. 7 Pseudo-second order rate constants for adsorption of zinc ion onto natural HAP

TABLE II
THE LANGMUIR CONSTANTS FOR ADSORPTION OF ZINC IONS ONTO NATURAL HAP

<table>
<thead>
<tr>
<th>Particle Size</th>
<th>ph</th>
<th>qmax (mmol/g)</th>
<th>b(L/g)</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>1537.6 nm</td>
<td>4.50</td>
<td>1.051</td>
<td>3.610</td>
<td>0.963</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>1.114</td>
<td>4.007</td>
<td>0.972</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>1.310</td>
<td>3.454</td>
<td>0.982</td>
</tr>
<tr>
<td>47.6 nm</td>
<td>4.50</td>
<td>1.184</td>
<td>3.433</td>
<td>0.949</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>1.410</td>
<td>3.426</td>
<td>0.969</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>1.562</td>
<td>5.983</td>
<td>0.986</td>
</tr>
</tbody>
</table>

TABLE III
FREUNDLICH ISOTHERM CONSTANTS FOR ADSORPTION OF ZINC IONS ONTO NATURAL HAP

<table>
<thead>
<tr>
<th>Particle Size</th>
<th>ph</th>
<th>Kf (mmol/g)</th>
<th>b (L/g)</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>1537.6 nm</td>
<td>4.50</td>
<td>0.725</td>
<td>1.185</td>
<td>0.985</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>0.79</td>
<td>1.579</td>
<td>0.993</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>0.624</td>
<td>1.857</td>
<td>0.996</td>
</tr>
<tr>
<td>47.6 nm</td>
<td>4.50</td>
<td>0.782</td>
<td>1.713</td>
<td>0.989</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>0.77</td>
<td>1.861</td>
<td>0.991</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>0.761</td>
<td>2.954</td>
<td>0.995</td>
</tr>
</tbody>
</table>

TABLE IV
R² FOR INITIAL CONCENTRATION OF 0.1 MMOL/L

<table>
<thead>
<tr>
<th>Particle Size</th>
<th>ph</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>1537.6 nm</td>
<td>4.50</td>
<td>0.743</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>0.713</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>0.753</td>
</tr>
<tr>
<td>47.6 nm</td>
<td>4.50</td>
<td>0.744</td>
</tr>
<tr>
<td></td>
<td>6.00</td>
<td>0.753</td>
</tr>
<tr>
<td></td>
<td>7.50</td>
<td>0.625</td>
</tr>
</tbody>
</table>
TABLE V
PSEUDO-FIRST AND SECOND ORDER RATE CONSTANTS FOR ADSORPTION OF ZINC IONS ONTO NATURAL HAP

<table>
<thead>
<tr>
<th>Sorbent</th>
<th>Pseudo-first-order rate constants</th>
<th>Pseudo-second-order rate constants</th>
</tr>
</thead>
<tbody>
<tr>
<td>Natural HAP</td>
<td>$k_1$(1/min) 0.004</td>
<td>$k_2$($g$mmol$^{-1}$min$^{-1}$) 0.038</td>
</tr>
</tbody>
</table>

TABLE VI
THERMODYNAMIC PARAMETERS OF ZINC SORPTION ON NATURAL HAP ($\Delta H^°$ & $\Delta S^°$)

<table>
<thead>
<tr>
<th>N-HAP size</th>
<th>$\Delta H^°$ (KJ mol$^{-1}$)</th>
<th>$\Delta S^°$ (KJ mol$^{-1}$K$^{-1}$)</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1537.6 nm</td>
<td>6.370</td>
<td>32.83</td>
<td>0.977</td>
</tr>
<tr>
<td>47.6 nm</td>
<td>8.194</td>
<td>39.96</td>
<td>0.993</td>
</tr>
</tbody>
</table>

TABLE VII
THERMODYNAMIC PARAMETERS OF THE ZINC ION SORPTION ON NATURAL HAP ($\Delta G^°$)

<table>
<thead>
<tr>
<th>N-HAP size</th>
<th>$K_2$</th>
<th>$-\Delta G^°$(KJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1537.6 nm</td>
<td>6.370</td>
<td>32.83</td>
</tr>
<tr>
<td>47.6 nm</td>
<td>8.194</td>
<td>39.96</td>
</tr>
</tbody>
</table>

B. Kinetic Studies

The maximum efficiency of N-HAP in sorption of the Zn (II) ion obtained at pH=7.50 and for the 47.6 nm particle size was about 88% (Fig. 5). The results show lower adsorption in comparison to recent researches which were carried out by commercial HAP.

The difference in adsorption results may have two reasons:
1) Using N-HAP instead of commercial HAP.
2) The difference between the dosage of N-HAP used in these experiments and that of previous researches.

With the plot $\log(q_e - q_t)$ versus time, the values of $k_1$ can be determined. The slopes and intercepts of plots $t$/$q_t$ versus $t$ were used to calculate the second-order rate constants $k_2$ and $q_e$. As can be seen from Figs. 6 and 7, the results obtained for the adsorption of Zn (II) ion onto N-HAP were fitted to Eqs. (11) and (12), and an approximate linear fit was observed. The values of $k_1$, $k_2$, and $R^2$, shown in Table 5, clearly indicate the pseudo second-order model provided better correlation coefficients than the pseudo first-order model for adsorption of zinc ions onto N-HAP, which suggests that this adsorption system is not a first-order kinetic adsorption process.

Therefore, the zinc ion adsorption onto the N-HAP belongs to the second-order kinetic model and the adsorption is a chemical process.

C. Thermodynamic Studies

Plotting $\ln K_0$ versus $1/T$ gives a straight line with a slope and intercept equal to $-\Delta H^°/R$ and $\Delta S^°/R$, respectively. The values of $\Delta H^°$ was positive, indicating that the sorption reaction was endothermic. The positive value of $\Delta S^°$ during the zinc ion sorption indicates that there was an increase in the randomness in the solid/solution interface during the adsorption process.

The plot of $\ln$Ln $S^*$ versus $1/T$ will give a linear plot with an intercept of $\ln S^*$ and a slope of $E_a/R$ (Fig. 9) as shown in Table 8. The value of $S^*$ was found to be 0.1, which is very close to zero, indicating that the adsorption follows 5hemisorptions [19].

IV. CONCLUSIONS

In this study, sorption experiments of the Zn (II) ion onto N-HAP, extracted from bovine ash, were used for the removal of this metal ion from aqueous solutions. The sorption behaviors of Zinc ions in these experiments under various conditions were examined and the following conclusions can be made:
1. The maximum sorption capacity and effect of N-HAP increases as pH increases from 4.50 to 7.50 and it has the best value of 1.310 and 1.562 mmol/g at pH=7.50 for 1537.6 nm and 47.6 nm particle sizes, respectively.
2. Sorption of Zinc ion onto N-HAP follows the second-order rate kinetics.
3. The Freundlich isotherm model is appropriate to describe the sorption of the Zn (II) ion on the N-HAP and it has a better fit than the Langmuir isotherm model.
4. In 47.6 nm particle sizes, these experiments show better maximum sorption capacity and more appropriate thermodynamic parameters.
5. Values of $\Delta G^°$ show that the sorption of the Zn (II) ion onto N-HAP is a favorable spontaneous process.
6. The values of $S^*$ show that adsorption follows 5hemisorptions.
7. The values of $\Delta H^°$ and $\Delta S^°$ are 8.194 KJ.mol$^{-1}$ and 39.96 KJ.mol$^{-1}$.K$^{-1}$, respectively, which indicate an endothermic sorption process and an increase in the randomness in the solid/solution interface during the sorption process.

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REFERENCES


