Fruitful functions

5.1. Return values

The built-in functions we have used, such as abs, pow, and max, have produced results. Calling each of these functions generates a value, which we usually assign to a variable or use as part of an expression.

\[
\begin{align*}
\text{biggest} &= \max(3, 7, 2, 5) \\
x &= \abs{3 - 11} + 10
\end{align*}
\]

But so far, none of the functions we have written has returned a value.

In this chapter, we are going to write functions that return values, which we will call fruitful functions, for want of a better name. The first example is area, which returns the area of a circle with the given radius:

```
def area(radius):
    temp = 3.14159 * radius**2
    return temp
```

We have seen the return statement before, but in a fruitful function the return statement includes a return value. This statement means: Return immediately from this function and use the following expression as a return value. The expression provided can be arbitrarily complicated, so we could have written this function more concisely:

```
def area(radius):
    return 3.14159 * radius**2
```

On the other hand, temporary variables like temp often make debugging easier.

Sometimes it is useful to have multiple return statements, one in each branch of a conditional. We have already seen the built-in abs, now we see how to write our own:

```
def absolute_value(x):
    if x < 0:
        return -x
    else:
        return x
```
Since these return statements are in an alternative conditional, only one will be executed. As soon as one is executed, the function terminates without executing any subsequent statements.

Another way to write the above function is to leave out the else and just follow the if condition by the second return statement.

```python
def absolute_value(x):
    if x < 0:
        return -x
    return x
```

Think about this version and convince yourself it works the same as the first one.

Code that appears after a return statement, or any other place the flow of execution can never reach, is called **dead code**.

In a fruitful function, it is a good idea to ensure that every possible path through the program hits a return statement. The following version of `absolute_value` fails to do this:

```python
def absolute_value(x):
    if x < 0:
        return -x
    elif x > 0:
        return x
```

This version is not correct because if `x` happens to be 0, neither condition is true, and the function ends without hitting a return statement. In this case, the return value is a special value called **None**:

```python
>>> print absolute_value(0)
None
```

None is the unique value of a type called the `NoneType`:

```python
>>> type(None)
```

All Python functions return None whenever they do not return another value.
5.2. Program development

At this point, you should be able to look at complete functions and tell what they do. Also, if you have been doing the exercises, you have written some small functions. As you write larger functions, you might start to have more difficulty, especially with runtime and semantic errors.

To deal with increasingly complex programs, we are going to suggest a technique called **incremental development**. The goal of incremental development is to avoid long debugging sessions by adding and testing only a small amount of code at a time.

As an example, suppose you want to find the distance between two points, given by the coordinates \((x_1, y_1)\) and \((x_2, y_2)\). By the Pythagorean theorem, the distance is:

\[
distance = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}
\]

The first step is to consider what a distance function should look like in Python. In other words, what are the inputs (parameters) and what is the output (return value)?

In this case, the two points are the inputs, which we can represent using four parameters. The return value is the distance, which is a floating-point value.

Already we can write an outline of the function:

```python
def distance(x1, y1, x2, y2):
    return 0.0
```

Obviously, this version of the function doesn’t compute distances; it always returns zero. But it is syntactically correct, and it will run, which means that we can test it before we make it more complicated.

To test the new function, we call it with sample values:

```python
>>> distance(1, 2, 4, 6)
0.0
```

We chose these values so that the horizontal distance equals 3 and the vertical distance equals 4; that way, the result is 5 (the hypotenuse of a 3–4–5 triangle). When testing a function, it is useful to know the right answer.
At this point we have confirmed that the function is syntactically correct, and we can start adding lines of code. After each incremental change, we test the function again. If an error occurs at any point, we know where it must be — in the last line we added.

A logical first step in the computation is to find the differences \(x_2 - x_1\) and \(y_2 - y_1\). We will store those values in temporary variables named \(dx\) and \(dy\) and print them.

```python
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    print "dx is", dx
    print "dy is", dy
    return 0.0
```

If the function is working, the outputs should be 3 and 4. If so, we know that the function is getting the right parameters and performing the first computation correctly. If not, there are only a few lines to check.

Next we compute the sum of squares of \(dx\) and \(dy\):

```python
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    dsquared = dx**2 + dy**2
    print "dsquared is: ", dsquared
    return 0.0
```

Notice that we removed the print statements we wrote in the previous step. Code like that is called **scaffolding** because it is helpful for building the program but is not part of the final product.

Again, we would run the program at this stage and check the output (which should be 25).

Finally, using the fractional exponent 0.5 to find the square root, we compute and return the result:

```python
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
```
dsquared = dx**2 + dy**2
result = dsquared**0.5
return result

If that works correctly, you are done. Otherwise, you might want to print the value of result before the return statement.

When you start out, you should add only a line or two of code at a time. As you gain more experience, you might find yourself writing and debugging bigger chunks. Either way, the incremental development process can save you a lot of debugging time.

The key aspects of the process are:

1. Start with a working program and make small incremental changes. At any point, if there is an error, you will know exactly where it is.
2. Use temporary variables to hold intermediate values so you can output and check them.
3. Once the program is working, you might want to remove some of the scaffolding or consolidate multiple statements into compound expressions, but only if it does not make the program difficult to read.

5.3. Composition

As you should expect by now, you can call one function from within another. This ability is called composition.

As an example, we’ll write a function that takes two points, the center of the circle and a point on the perimeter, and computes the area of the circle.

Assume that the center point is stored in the variables xc and yc, and the perimeter point is in xp and yp. The first step is to find the radius of the circle, which is the distance between the two points. Fortunately, we’ve just written a function, distance, that does just that, so now all we have to do is use it:

radius = distance(xc, yc, xp, yp)

The second step is to find the area of a circle with that radius and return it. Again we will use one of our earlier functions:

result = area(radius)
Wrapping that up in a function, we get:

```python
def area2(xc, yc, xp, yp):
    radius = distance(xc, yc, xp, yp)
    result = area(radius)
    return result
```

We called this function `area2` to distinguish it from the `area` function defined earlier. There can only be one function with a given name within a given module.

The temporary variables `radius` and `result` are useful for development and debugging, but once the program is working, we can make it more concise by composing the function calls:

```python
def area2(xc, yc, xp, yp):
    return area(distance(xc, yc, xp, yp))
```

### 5.4. Boolean functions

Functions can return boolean values, which is often convenient for hiding complicated tests inside functions. For example:

```python
def is_divisible(x, y):
    if x % y == 0:
        return True
    else:
        return False
```

The name of this function is `is_divisible`. It is common to give **boolean functions** names that sound like yes/no questions. `is_divisible` returns either True or False to indicate whether the `x` is or is not divisible by `y`.

We can make the function more concise by taking advantage of the fact that the condition of the if statement is itself a boolean expression. We can return it directly, avoiding the if statement altogether:

```python
def is_divisible(x, y):
    return x % y == 0
```
return \( x \% y == 0 \)

This session shows the new function in action:

```python
>>> is_divisible(6, 4)
False
>>> is_divisible(6, 3)
True
```

Boolean functions are often used in conditional statements:

```python
if is_divisible(x, y):
    print "x is divisible by y"
else:
    print "x is not divisible by y"
```

It might be tempting to write something like:

```python
if is_divisible(x, y) == True:
```

but the extra comparison is unnecessary.

### 5.5. The function type

A function is another type in Python, joining `int`, `float`, `str`, `bool`, and `NoneType`.

```python
>>> def func():
     ...     return "function func was called..."
     ...
>>> type(func)
<type 'function'>
```

Just like the other types, functions can be passed as arguments to other functions:

```python
def f(n):
    return 3*n - 6

def g(n):
    return 5*n + 2
```
```python
def h(n):
    return -2*n + 17
def doto(value, func):
    return func(value)

print doto(7, f)
print doto(7, g)
print doto(7, h)
```
doto is called three times. 7 is the argument for value each time, and the functions f, g, and h are passed in for func in turn. The output of this script is:

```
15
37
3
```

This example is a bit contrived, but we will see situations later where it is quite useful to pass a function to a function.

5.6. Programming with style

Readability is very important to programmers, since in practice programs are read and modified far more often than they are written. All the code examples in this book will be consistent with the [Python Enhancement Proposal 8 (PEP 8)](https://legacy.python.org/dev/peps/pep-0008), a style guide developed by the Python community.

We'll have more to say about style as our programs become more complex, but a few pointers will be helpful already:

- use 4 spaces for indentation
- imports should go at the top of the file
- separate function definitions with two blank lines
- keep function definitions together
- keep top level statements, including function calls, together at the bottom of the program

5.7. Triple quoted strings
In addition to the single and double quoted strings we first saw in *Values and data types*, Python also has *triple quoted strings*:

```python
>>> type('''This is a triple quoted string using 3 double quotes.''')
<type 'str'>
>>> type('''This triple quoted strings uses 3 single quotes.'''
<type 'str'>
```

Triple quoted strings can contain both single and double quotes inside them:

```python
>>> print """Oh no", she exclaimed, "Ben's bike is broken!""
"Oh no", she exclaimed, "Ben's bike is broken!"
```

Finally, triple quoted strings can span multiple lines:

```python
>>> message = """This message will
... span several
... lines.""
>>> print message
This message will
span several
lines.
```

5.8. Unit testing with doctest

It is a common best practice in software development these days to include automatic **unit testing** of source code. Unit testing provides a way to automatically verify that individual pieces of code, such as functions, are working properly. This makes it possible to change the implementation of a function at a later time and quickly test that it still does what it was intended to do.

Python has a built-in doctest module for easy unit testing. Doctests can be written within a triple quoted string on the first line of the body of a function or script. They consist of sample interpreter sessions with a series of inputs to a Python prompt followed by the expected output from the Python interpreter.
The doctest module automatically runs any statement beginning with >>> and compares the following line with the output from the interpreter.

To see how this works, put the following in a script named myfunctions.py:

```python
def is_divisible_by_2_or_5(n):
    
    >>> is_divisible_by_2_or_5(8)
    True

if __name__ == '__main__':
    import doctest
    doctest.testmod()
```

The last three lines are what make doctest run. Put them at the bottom of any file that includes doctests. We will explain how they work in Chapter 10 when we discuss modules.

Running the script will produce the following output:

```
$ python myfunctions.py
********************************************************************
File "myfunctions.py", line 3, in __main__.is_divisible_by_2_or_5
Failed example:
    is_divisible_by_2_or_5(8)
Expected:
    True
Got nothing
********************************************************************
1 items had failures:
    1 of  1 in __main__.is_divisible_by_2_or_5
***Test Failed*** 1 failures.
```

This is an example of a failing test. The test says: if you call is_divisible_by_2_or_5(8) the result should be True. Since is_divisible_by_2_or_5 as written doesn’t return anything at all, the test fails, and doctest tells us that it expected True but got nothing.
We can make this test pass by returning True:

```python
def is_divisible_by_2_or_5(n):
    """
    >>> is_divisible_by_2_or_5(8)
    True
    """
    return True
```

If we run it now, there will be no output, which indicates that the test passed. Note again that the doctest string must be placed immediately after the function definition header in order to run.

To see more detailed output, call the script with the `-v` command line option:

```
$ python myfunctions.py -v
Trying:
    is_divisible_by_2_or_5(8)
Expecting:
    True
ok
1 items had no tests:
    __main__
1 items passed all tests:
    1 tests in __main__.is_divisible_by_2_or_5
1 tests in 2 items.
1 passed and 0 failed.
Test passed.
```

While the test passed, our test suite is clearly inadequate, since `is_divisible_by_2_or_5` will now return True no matter what argument is passed to it. Here is a completed version with a more complete test suite and code that makes the tests pass:
def is_divisible_by_2_or_5(n):
    """
    >>> is_divisible_by_2_or_5(8)
    True
    >>> is_divisible_by_2_or_5(7)
    False
    >>> is_divisible_by_2_or_5(5)
    True
    >>> is_divisible_by_2_or_5(9)
    False
    """
    return n % 2 == 0 or n % 5 == 0

if __name__ == '__main__':
    import doctest
    doctest.testmod()

Run this script now with the -v command line option and see what you get.

5.9. Glossary

boolean function
A function that returns a boolean value.

composition (of functions)
Calling one function from within the body of another, or using the return value of one function as an argument to the call of another.

dead code
Part of a program that can never be executed, often because it appears after a return statement.

fruitful function
A function that yields a return value.

incremental development
A program development plan intended to avoid debugging by adding and testing only a small amount of code at a time.

None
A special Python value returned by functions that have no return statement, or a return statement without an argument. None is the only value of the type, NoneType.

**return value**
The value provided as the result of a function call.

**scaffolding**
Code that is used during program development but is not part of the final version.

**temporary variable**
A variable used to store an intermediate value in a complex calculation.

**unit testing**
An automatic procedure used to validate that individual units of code are working properly. Python has doctest built in for this purpose.

### 5.10. Exercises

All of the exercises below should be added to a file named ch05.py that contains the following at the bottom:

```python
if __name__ == '__main__':
    import doctest
doctest.testmod()
```

After completing each exercise in turn, run the program to confirm that the doctests for your new function pass.

Write a compare function that returns 1 if \( a > b \), 0 if \( a == b \), and \(-1\) if \( a < b \).

```python
def compare(a, b):
    """
    >>> compare(5, 4)
    1
    >>> compare(7, 7)
    0
    >>> compare(2, 3)
    -1
    >>> compare(42, 1)
    1
    """
    # Your function body should begin here.
```
Fill in the body of the function so the doctests pass.

Use incremental development to write a function called hypotenuse that returns the length of the hypotenuse of a right triangle given the lengths of the two legs as parameters. Record each stage of the incremental development process as you go.

```python
def hypotenuse(a, b):
    """
    >>> hypotenuse(3, 4)
    5.0
    >>> hypotenuse(12, 5)
    13.0
    >>> hypotenuse(7, 24)
    25.0
    >>> hypotenuse(9, 12)
    15.0
    """

When you are finished add your completed function with the doctests to ch05.py and confirm that the doctests pass.

Write a function slope(x1, y1, x2, y2) that returns the slope of the line through the points (x1, y1) and (x2, y2). Be sure your implementation of slope can pass the following doctests:

```python
def slope(x1, y1, x2, y2):
    """
    >>> slope(5, 3, 4, 2)
    1.0
    >>> slope(1, 2, 3, 2)
    0.0
    >>> slope(1, 2, 3, 3)
    0.5
    >>> slope(2, 4, 1, 2)
    2.0
    """
```

Then a call to slope in a new function named intercept(x1, y1, x2, y2) that returns the y–intercept of the line through the points (x1, y1) and (x2, y2).
def intercept(x1, y1, x2, y2):
    """
    >>> intercept(1, 6, 3, 12)
    3.0
    >>> intercept(6, 1, 1, 6)
    7.0
    >>> intercept(4, 6, 12, 8)
    5.0
    """

intercept should pass the doctests above.

Write a function called is_even(n) that takes an integer as an argument and returns True if the argument is an even number and False if it is odd.

Add your own doctests to this function.

Now write the function is_odd(n) that returns True when n is odd and False otherwise. Include doctests for this function as you write it.

Finally, modify it so that it uses a call to is_even to determine if its argument is an odd integer.

Add the following function definition header and doctests to ch05.py:

def is_factor(f, n):
    """
    >>> is_factor(3, 12)
    True
    >>> is_factor(5, 12)
    False
    >>> is_factor(7, 14)
    True
    >>> is_factor(2, 14)
    True
    >>> is_factor(7, 15)
    False
    """
Add a body to `is_factor` to make the doctests pass.

Add the following function definition header and doctests to `ch05.py`:

```python
def is_multiple(m, n):
    
    >>> is_multiple(12, 3)
    True
    >>> is_multiple(12, 4)
    True
    >>> is_multiple(12, 5)
    False
    >>> is_multiple(12, 6)
    True
    >>> is_multiple(12, 7)
    False

Add a body to `is_multiple` to make the doctests pass. Can you find a way to use `is_factor` in your definition of `is_multiple`?

Add the following function definition header and doctests to `ch05.py`:

```python
def f2c(t):
    
    >>> f2c(212)
    100
    >>> f2c(32)
    0
    >>> f2c(-40)
    -40
    >>> f2c(36)
    2
    >>> f2c(37)
    3
    >>> f2c(38)
    3
    >>> f2c(39)
    4
```
Write a body for the function definition of f2c designed to return the integer value of the nearest degree Celsius for given temperature in Fahrenheit. (*hint:* you may want to make use of the built-in function, round. Try printing `round.__doc__` in a Python shell and experimenting with `round` until you are comfortable with how it works.)

Add the following function definition header and doctests to `ch05.py`:

```python
def c2f(t):
   
   >>> c2f(0)
   32
   >>> c2f(100)
   212
   >>> c2f(-40)
   -40
   >>> c2f(12)
   54
   >>> c2f(18)
   64
   >>> c2f(-48)
   -54
```

Add a function body for `c2f` to convert from Celsius to Fahrenheit.

*Source: http://openbookproject.net/thinkcs/python/english2e/ch05.html*