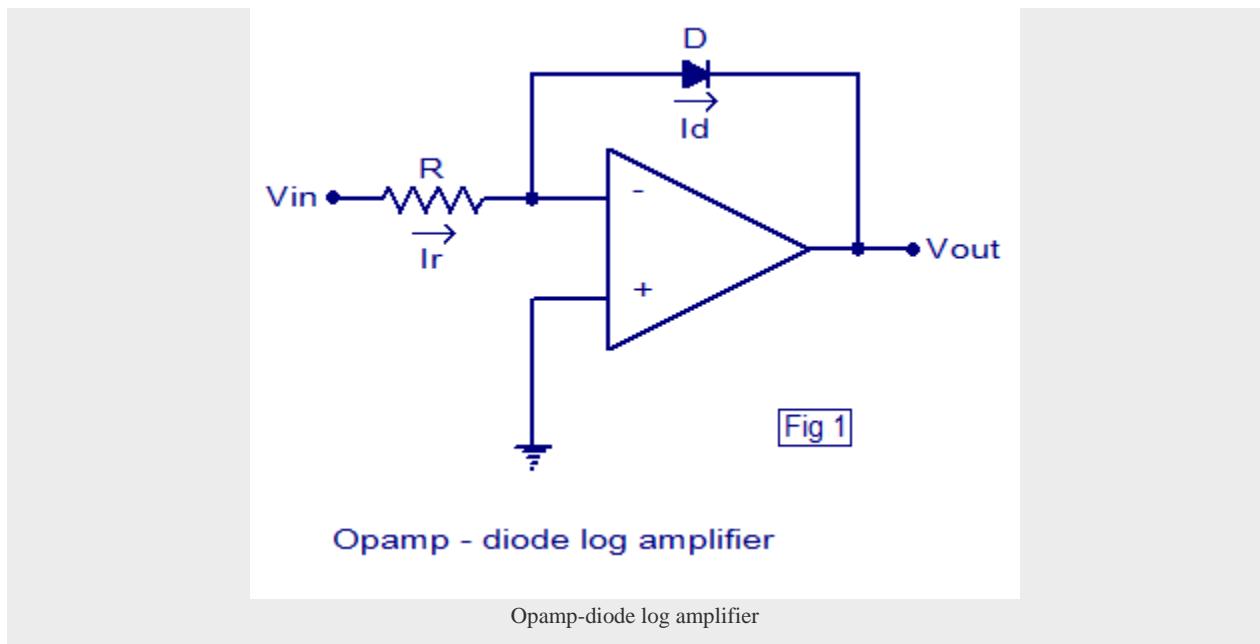


# LOG AMPLIFIER

## Log amplifier

Log amplifier is a linear circuit in which the output voltage will be a constant times the natural logarithm of the input. The basic output equation of a log amplifier is  $V_{out} = K \ln (V_{in}/V_{ref})$ ; where  $V_{ref}$  is the constant of normalisation, and  $K$  is the scale factor. Log amplifier finds a lot of application in electronic fields like multiplication or division (they can be performed by the addition and subtraction of the logs of the operand), signal processing, computerised process control, compression, decompression, RMS value detection etc. Basically there are two log amp configurations: Opamp-diode log amplifier and Opamp-transistor log.

### Opamp-diode log amplifier.



The schematic of a simple Opamp-diode log amplifier is shown above. This is nothing but an opamp wired in closed loop inverting configuration with a diode in the feedback path. The voltage across the diode will be always proportional to the log of the current through it and when a diode is placed in the feedback path of an opamp in inverting mode, the output voltage will be proportional to the negative log of the input current. Since the input current is proportional to the input voltage, we can say that the output voltage will be proportional to the negative log of the input voltage.

According to the PN junction diode equation, the relationship between current and voltage for a diode is

$$I_d = I_s (e^{(V_d/V_t)} - 1) \dots \dots \dots (1)$$

Where  $I_d$  is the diode current,  $I_s$  is the saturation current,  $V_d$  is the voltage across the diode and  $V_t$  is the thermal voltage.

Since  $V_d$  the voltage across the diode is positive here and  $V_t$  the thermal voltage is a small quantity, the equation (1) can be approximated as

$$I_d = I_s e^{(V_d/V_t)} \dots\dots\dots(2)$$

Since an ideal opamp has infinite input resistance, the input current  $I_r$  has only one path, that is through the diode. That means the input current is equal to the diode current  $I_d$ .

$$\Rightarrow I_r = I_d \dots\dots\dots(3)$$

Since the inverting input pin of the opamp is virtually grounded, we can say that

$$I_r = V_{in}/R$$

Since  $I_r = I_d$  (from equation (3) )

$$V_{in}/R = I_d \dots\dots\dots(4)$$

Comparing equation (4) and (2) we have

$$V_{in}/R = I_s e^{(V_d/V_t)}$$

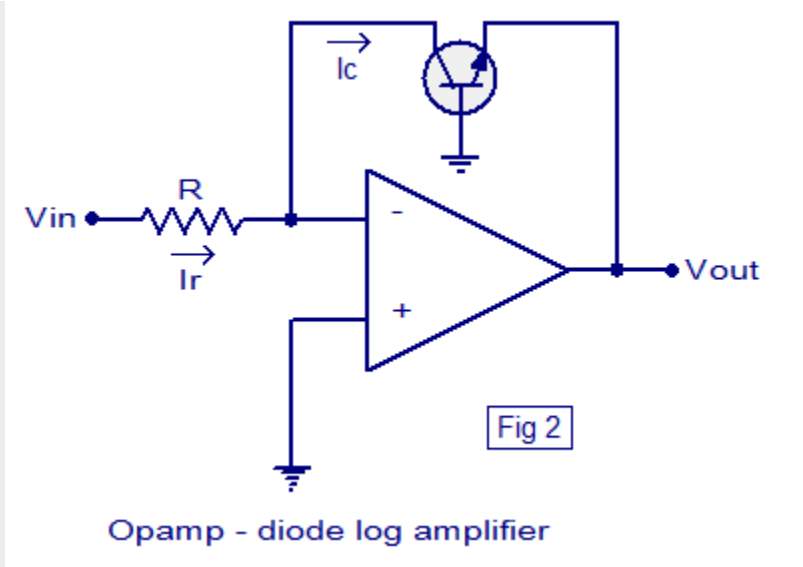
$$\text{i.e. } V_{in} = I_s R e^{(V_d/V_t)} \dots\dots\dots(5)$$

Considering that the negative of the voltage across diode is the output voltage  $V_{out}$  (see the circuit diagram (fig1)), we can rearrange the equation (5) to get

$$V_{out} = -V_t \ln(V_{in}/I_s R)$$

### Opamp transistor log amplifier.

In this configuration a transistor is placed in the feedback path of an opamp wired in inverting mode. Collector of the transistor is connected to the inverting input of the opamp, emitter to output and base is grounded. The necessary condition for a log amp to work is that the input voltage must be always positive. Circuit diagram of an Opamp-transistor log amplifier is shown below.



Opamp-transistor log amplifier

From Fig 2 it is clear that base-emitter voltage of the transistor  $V_{be} = -V_{out}$  .....(1)

We know that  $I_c = I_{so} (e^{(V_{be}/V_t)} - 1)$  .....(2)

Where  $I_c$  is the collector current of the transistor,  $I_{so}$  the saturation current,  $V_{be}$  the base emitter voltage and  $V_t$  the thermal voltage.

Equation (1) can be approximated as  $I_c = I_{so} e^{(V_{be}/V_t)}$  .....(3)

ie,  $V_{be} = V_t \ln (I_c/I_{so})$  .....(4)

Since input pin of an ideal opamp has infinite input impedance, the only path for the input current  $I_r$  is through the transistor and that means  $I_r = I_c$ .

Since the inverting input of the opamp is virtually grounded

$I_r = V_{in}/R$

That means  $I_c = V_{in}/R$  .....(5)

From equations (5) , (4) and (1) it is clear that

$V_{out} = -V_t \ln (V_{in}/I_{so}R)$ .....(6)

Source : <http://www.circuitstoday.com/log-amplifier>