

## Design of High Performance Modified Wave pipelined DAA Filter with Critical Path Approach

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### I. INTRODUCTION

The complexity in digital circuits is growing day by day, reducing delay and a proper clocking methodology is

very important to maintain the overall system performance. The designers have always been trying to reduce the total

delay of a circuit to make the design faster. But the modern CMOS technology, where time is required to transfer some logic from input to output of a gate is typically less than 1 ns, while the overall system clock period remains greater than 10 ns. This implies 10% logic utilization, i.e. at any particular instance of time, 90% of the logic gates become idle. So, it can be maximized by utilizing this idle time and can be achieved by using wave pipelining technique.

In case of ordinary pipeline system, there is one wave of data between register stages. When a new set of data has been clocked into one set of register, the values are propagated to the next stage of register before the first set of data has been clocked again. By this technique the speed will be improved but at the cost of increased number of registers, area, latency, power.

But in case of Wave pipelining (WP) system; multiple waves of data are propagated between storage elements. It was first introduced by cotton who named it maximum rate pipelining. He observed that the rate at which logic can propagate through a circuit depend not only on the longest path delay but also on the difference between the longest and shortest path delay. As a result, several computational “waves”, i.e., logic signals related to different clock cycles, can propagate through the logic simultaneously. The operating speed can be increased in wave pipelining technique by adjustment of clock period, adjustment of clock skew and equalization of path delay. In this paper a new high speed control circuit is introduced which will act as critical path.

### II. OVERVIEW

Wave Pipelining is a combinational logic circuit design technique which is implementing pipelining without the use of storage or sequential elements. Traditional pipelining is done by inserting flip flops between different intermediate stages of the circuit, which are all clocked by a common clock signal. The maximum frequency of operation of these designs is

**Abstract—** In this paper, a new high speed control circuit is proposed which will act as a critical path for the data which will go from input to output to improve the performance of wave pipelining circuits. The wave pipelining is a method of high performance circuit designs which implements pipelining in logic without the use of intermediate registers. Wave pipelining has been widely used in the past few years with a great deal of significant features in technology and applications. It has the ability to improve speed, efficiency, economy in every aspect which it presents. Wave pipelining is being used in wide range of applications like digital filters, network routers, multipliers, fast convolvers, MODEMs, image processing, control systems, radars and many others. In previous work, the operating speed of the wave-pipelined circuit can be increased by the following three tasks: adjustment of the clock period, clock skew and equalization of path delays. The path-delay equalization task can be done theoretically, but the real challenge is to accomplish it in the presence of various different delays. So, the main objective of this paper is to solve the path delay equalization problem by inserting the control circuit in wave pipelined based circuit which will act as critical path for the data that moves from input to output. The proposed technique is evaluated for DSP applications by designing 4- tap FIR filter using Distributed arithmetic algorithm (DAA). Then comparison of this design is done with 4-tap FIR filter designs using conventional pipelining and non pipelining. The synthesis and simulation results based on Xilinx ISE Navigator 12.3 shows that wave pipelined DAA based filter is faster by a factor of 1.43 compared to non pipelined one and the conventional pipelined filter is faster than non pipelined by factor of 1.61 but at the cost of increased logic utilization by 200 %. So, the wave-pipelined DA filters designed with the proposed control circuit can operate at higher frequency than that of non-pipelined but less than that of pipelined. The gain in speed in pipelined compared to that of wave-pipelined is at the cost of increased area and more dissipated power. When latency is considered, wave-pipelined design filters with the proposed scheme are having the lowest latency among three schemes designed.

**Keywords—**control circuit, DAA, wave pipelining, FIR, critical path

determined by the worst case delay path and the setup & hold time requirements of the flip flops. This can prove to be a bottleneck to the maximum frequency of operation of the circuit

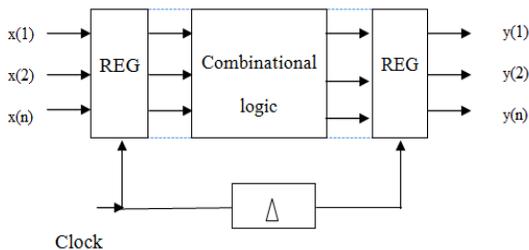


Fig 1. A combinational logic circuit with I/O registers

Cotten [12] has proved that the maximum rate at which data logic can propagate through the circuit depends on  $(D_{max} - D_{min})$  where  $D_{max}$  and  $D_{min}$  represent the maximum and minimum propagation delay of the circuit and not just on the maximum propagation delay. Hence, Cotten proposed that decreasing the value of  $(D_{max} - D_{min})$  will increase the maximum at which data can propagate and called it Maximum Rate Pipelining[12]. Figure 1 is a block diagram representation of wave pipelining. In this figure, the skew  $\Delta = (D_{max} - D_{min})$ .

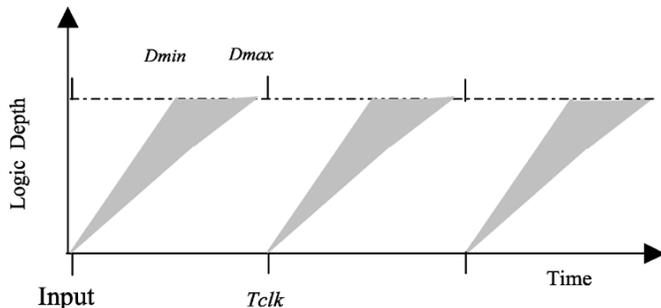


Fig2. Temporal/spatial diagram of combinational logic circuit

### III. REVIEW OF RELATED WORK

Wave-pipelining is proposed as one of the techniques for achieving high speed without the cost of increased area and circuit complexity. In this, the main function is partitioned into many independent but interconnected sub-functions, and these sub-functions are processed in each stage of the circuit. The basic criteria used for partitioning the execution path into stages is to have stages with nearly equal computation delay, so that all the stages can be kept busy during entire length of clock cycle. This criterion is hard to achieve in practice because of the differing amounts of logic per stage and variations in time delays per logic element. The concept of wave-pipelining has been described in a number of previous works[2][3][7][20].

There are many ways of implementing wave-pipelined circuits. In these circuits, main task is to equalizing or balancing path delay  $(D_{max} - D_{min})$  to maximizing the speed. Previously to maximizing operating speed of the wave-pipelined circuit, adjustment of clock period, clock skew ( $\delta$ )

and equalization of path delays are the three tasks required. All three tasks require the delays to be measured and altered if required. So to design wave-pipelined circuits, it is necessary to balance the path delays. For practical circuits, usually the nominal path delay to be a predefined constant  $D_{max}$ . Because the circuit must interface to other components in the system. While in theory the path-delay equalization problem has been solved, the real challenge is to accomplish it in the presence of a variety of static and dynamic delay tolerances. So, balancing problem is major challenge for designers in these days. In this paper, to overcome this problem active delay elements are used in the circuit called control circuit and then inserted in the architecture. This process is also called rough tuning. This control circuit has a very high speed and it acts as critical path for the data moves from input to output. So it increases the overall operating frequency of the circuit.

### IV. PROPOSED CRITICAL PATH SCHEME

#### A. Concept of control circuit used for critical path scheme

Control circuit is basically a circuit consists of flip-flops and XOR gates[17]. It is basically high speed circuit. This circuit will be placed in the wave-pipelined architecture as shown in figure3 to improve the operating speed. In wave-pipelined circuit, data will move from input to output in different waves. In the previous work, designers calculated Maximum ( $D_{max}$ ) and minimum ( $D_{min}$ ) distance which varies from input to output. Then by taking the difference between these two distances ( $D_{max} - D_{min}$ ) they improves the speed. For this, firstly we have to calculate all the distances, after that maximum and minimum distance to be sort out. It is very time consuming process requires more hardware. The modified wave-pipelined circuit is as shown in Fig 3. In this, whatever the data will enter at the input X, the same data will be at output but at very high speed. The advantage of this circuit is that it is automatic high speed circuit which will automatically act as critical path for the data moving from input to output.

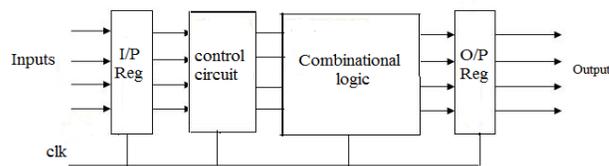


Fig 3 Modified wave-pipelined circuit with control circuit

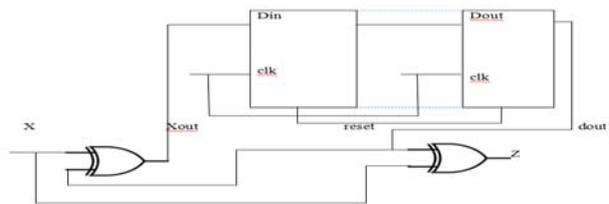


Fig 4 Control circuit having D flip-flops and XOR gates

## V. FIR THEORY

An FIR with constant coefficients is an LTI digital filter. The output of an FIR of order or length  $L$ , to an input time-series  $x[n]$ , is given by a finite version of the convolution sum given in (1.1), namely

$$y(n) = x(n) * f(n) = \sum_{k=0}^{L-1} f(k)x(n-k) \quad (1)$$

Where  $f[0] = 0$  through  $f[L-1] = 0$  are the filter's  $L$  coefficients. They also correspond to the FIR's impulse response. For LTI systems it is sometime more convenient to express in the  $z$ -domain with

$$Y(z) = F(z)X(z), \quad (2)$$

Where  $F(z)$  is the FIR's transfer function defined in the  $z$ -domain by

$$F(z) = \sum_{k=0}^{L-1} f[k]z^{-k} \quad (3)$$

The  $L$ th-order LTI FIR filter is graphically interpreted in Fig 5. It can be seen to consist of a collection of a "tapped delay line," adders, and multipliers. One of the operands presented to each multiplier is an FIR coefficient, often referred to as a tap weight for obvious reasons. Historically, the FIR filter is also known by the name transversal filter. The roots of polynomial  $F(z)$  in (3) define the zeros of the filter. The presence of only zeros is the reason that FIRs are sometimes called all zero filters.

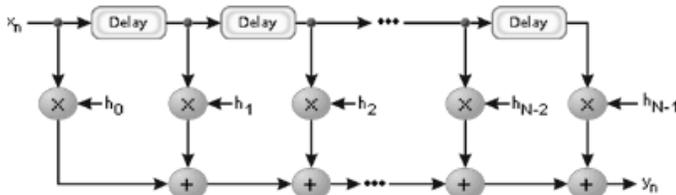


Fig 5. Direct form FIR filter [34].

## V1.DISTRIBUTED ARITHMETI ALGORITHM (DAA)

Distributed arithmetic (DA) was first introduced by Croisier et al and further developed by Peled and Lui. DA is a multiplier-less implementation for computing the inner product of a pair of vectors [8], a common computation used in digital signal processing. It is well suited to implementing high throughput FIR filters and signal transformations such as discrete cosine transforms or fast Fourier transforms. DA is a bit-serial computation that forms an inner product of a pair of vectors in a few steps by storing all possible combination sums

of weights in a memory table. It is assumed that the inputs to the filter are represented as B-bit 2's complement binary numbers with only the sign bit to the left of the radix point. A discrete-time linear finite impulse response filter generates the output  $y[n]$  as a sum of delayed and scaled input samples  $x[n]$ . In other words,

$$y[n] = \sum_{k=0}^{K-1} w_k x[n-1] \quad (4)$$

Let the signal samples to the filter be represented as B-bit 2's complement binary numbers,

$$x[n-1] = -b_{i0} + \sum_{k=0}^{K-1} b_{ik} 2^{-k} \quad (5)$$

where  $b_{il}$  is the  $l$ th bit in the 2's complement representation of  $x[n-i]$ . Substituting equation (5) into equation (4) and swapping the order of the summations yields

$$y[n] = -\sum_{i=0}^{K-1} b_{i0} w_i + \left[ \sum_{i=0}^{K-1} \sum_{k=0}^{K-1} b_{ik} w_i \right] 2^{-k} \quad (6)$$

For a given set of  $w_i$  ( $i = 0, \dots, K-1$ ), the terms in the square braces may take only one of  $2^K$  possible values, which may be stored in a memory table, denoted as the DA filtering memory table (DA-F-MEM). The entry in the DA-F-MEM addressed by  $r$ , is given by

$$DA-F-MEM_{[r]} = \sum_{i=0}^{K-1} c_i^{[r]} w_i \quad (7)$$

where  $c_i(r)$  is the  $i$ th bit in the  $K$ -bit representation of the address  $r$ .

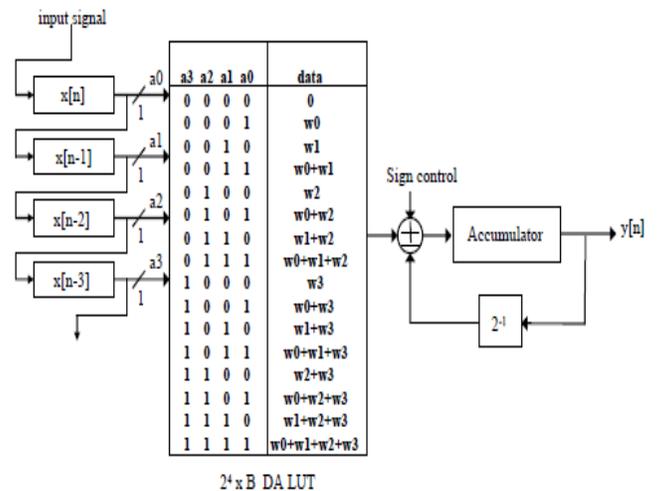


Fig 6. DA implementation of a 4-tap ( $K = 4$ ) FIR filter. [19]

A 4-tap ( $K = 4$ ) implementation of the DA FIR filter is shown in Fig 6. The DAF-MEM contains all 16 possible combination sums of the filter weights  $w_0, w_1, w_2,$  and  $w_3$ . The bank of shift registers in Fig. 6 stores 4 consecutive input samples ( $x[n - i], i=0, \dots, 3$ ). The concatenation of rightmost bits of the shift registers becomes the address of the memory table. The shift register is shifted right at every clock cycle. The corresponding memory table entries are also shifted and accumulated  $B$  consecutive times to generate the output  $y[n]$  where  $B$  is the precision of the input data. The sign bit control is used to change the addition to subtraction for the sign bits which are included in the first expression square brackets in equation (6). In addition, computing the filtering operation by utilizing the DA filter can be done in  $B$  clock cycles regardless of the size of the filter,  $K$ . Thus, obtaining a high throughput rate using the DA implementation, especially if  $K \gg B$ , is possible. Also due to the regular

### VII IMPLEMENTATION AND RESULTS

#### A. Implementation of 4 tap FIR filter using VERTAX 4 FPGA

A 4 tap FIR filter with 8-bit inputs and 8-bit coefficients as shown in fig.7 is implemented along with the proposed critical path approach in Vertax 4 FPGA using XILINX Project Navigator 12.3. Simulation results are also checked by using the same tool. The filter is implemented in three schemes: non-pipelined, pipelined and wave pipelined and comparisons are done in terms of operating frequency, area and latency. From the table 1 and Fig. 7, it can be observed that wave pipelined DA filter is faster by a factor of 1.43 compared to the non-pipelined DA filter. The Pipelined DA filter is faster by factor of 1.61 compared to the non pipelined DA filter. But this gain in speed is achieved at the cost of increased area. There is an increase in logic utilization by 200 %. Also the latency measured for the maximum operating frequency for wave-pipelined DA filter is the least compared to both non-pipelined and pipelined

TABLE 1 IMPLEMENTATION RESULTS FOR 4-TAP DA FILTER IN VERTAX 4

	Pipelining techniques		
	Wave pipelining	Non pipelining	Pipelining
Freq (MHz)	386.033	269.578	454.907
Slices	166	141	332
4 I/P LUT	308	216	324

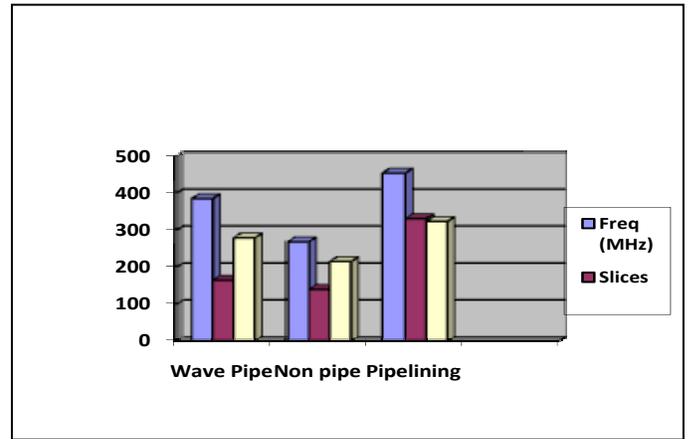


Fig.7 Comparison of speed and area of 4-tap DA filter

### VIII. CONCLUSION AND FUTURE SCOPE

In this paper, a new critical path approach to speeding up wave-pipelining technique for DAA based FIR filter using a control circuit has been presented. Previous results showed that wave pipelined DAA based FIR filter is faster by a factor of 1.36 compared to non pipelined techniques. In this work, the synthesis and simulation results based on Xilinx ISE Navigator 12.3 shows that wave pipelined DAA based filter is faster by a factor of 1.43 compared to non pipelined and the conventional pipelined filter is faster than non pipelined by factor of 1.61 but at the cost of increased logic utilization by 200%. So, the wave-pipelined DA filters designed with the proposed control circuit can operate at higher frequency than that of non-pipelined but less than that of pipelined. The gain in speed in conventional pipelined compared to that of wave-pipelined is at the cost of increased area. Moreover, power dissipation of pipelined circuits are higher than that of wave-pipelined circuits. When latency is considered, wave-pipelined design filters with the proposed scheme are having the lowest latency among three schemes designed. Results are showing that though area and power of wave-pipelined circuits are less than that of pipelined circuits but its performance is less than pipelined circuits.

So, in future further work can be done on wave pipelining technique to improve its performance.

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