

# SERIES AND PARALLEL RESISTORS

Resistors are paired together all the time in electronics, usually in either a series or parallel circuit. When resistors are combined in series or parallel, they create a **total resistance**, which can be calculated using one of two equations. Knowing how resistor values combine comes in handy if you need to create a specific resistor value.

## Series resistors

When connected in series resistor values simply add up.



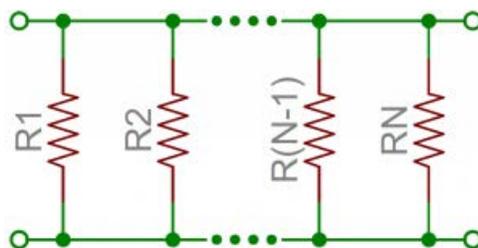
$$R_{tot} = R_1 + R_2 + \dots + R_{N-1} + R_N$$

*N resistors in series. The total resistance is the sum of all series resistors.*

So, for example, if you just *have to have* a 12.33k $\Omega$  resistor, seek out some of the more common resistor values of 12k $\Omega$  and 330 $\Omega$ , and butt them up together in series.

## Parallel resistors

Finding the resistance of resistors in parallel isn't quite so easy. The total resistance of  $N$  resistors in parallel is the inverse of the sum of all inverse resistances. This equation might make more sense than that last sentence:



$$\frac{1}{R_{tot}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_{N-1}} + \frac{1}{R_N}$$

*N resistors in parallel. To find the total resistance, invert each resistance value, add them up, and then invert that.*

(The inverse of resistance is actually called **conductance**, so put more succinctly: the *conductance* of parallel resistors is the sum of each of their conductances).

As a special case of this equation: if you have **just two** resistors in parallel, their total resistance can be calculated with this slightly-less-inverted equation:

$$R_{tot} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

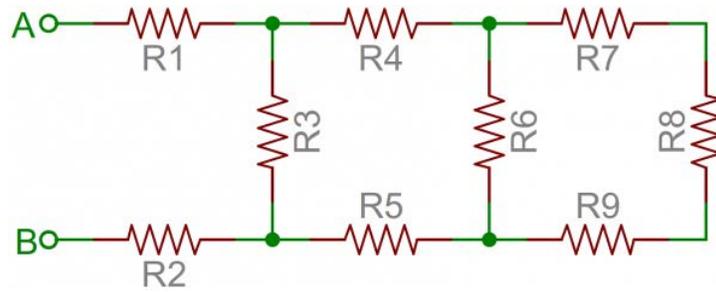
As an even *more special* case of that equation, if you have two parallel resistors of **equal value** the total resistance is half of their value. For example, if two 10kΩ resistors are in parallel, their total resistance is 5kΩ.

A shorthand way of saying two resistors are in parallel is by using the parallel operator: ||. For example, if R<sub>1</sub> is in parallel with R<sub>2</sub>, the conceptual equation could be written as R<sub>1</sub>||R<sub>2</sub>. Much cleaner, and hides all those nasty fractions!

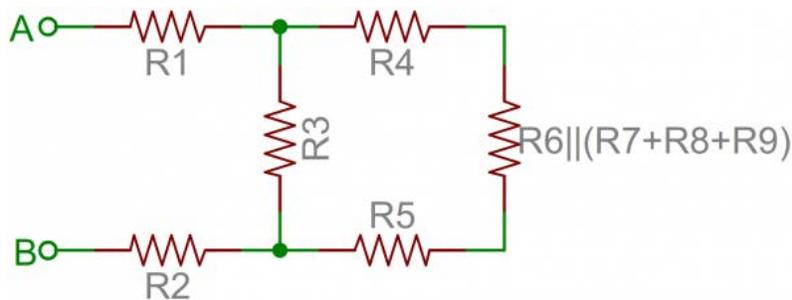
## Resistor networks

As a special introduction to calculating total resistances, electronics teachers just *love* to subject their students to finding that of crazy, convoluted resistor networks.

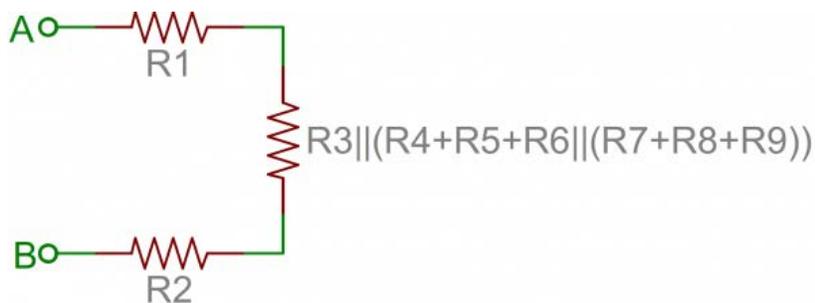
A tame resistor network question might be something like: “what’s the resistance from terminals *A* to *B* in this circuit?”



To solve such a problem, start at the back-end of the circuit and simplify towards the two terminals. In this case  $R_7$ ,  $R_8$  and  $R_9$  are all in series and can be added together. Those three resistors are in parallel with  $R_6$ , so those four resistors could be turned into one with a resistance of  $R_6 \parallel (R_7 + R_8 + R_9)$ . Making our circuit:



Now the four right-most resistors can be simplified even further.  $R_4$ ,  $R_5$  and our conglomeration of  $R_6 - R_9$  are all in series and can be added. Then those series resistors are all in parallel with  $R_3$ .



And that's just three series resistors between the  $A$  and  $B$  terminals. Add 'em on up! So the total resistance of that circuit is:  $R_1 + R_2 + R_3 \parallel (R_4 + R_5 + R_6 \parallel (R_7 + R_8 + R_9))$ .