SHAF for Mitigation of Current Harmonics Using p-q Method with PI and Fuzzy Controllers

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Abstract— Commencing with incandescent light bulb, every load today creates harmonics. Unfortunately, these loads vary with respect to their amount of harmonic content and response to problems caused by harmonics. The issue of harmonics is of great concern to engineers, building designers and also in industrial applications because they do not just distort voltage waveforms, but they can also overheat the building wiring, cause nuisance tripping, overheat transformer units, and cause random end-user equipment failures. Thus, power quality has become more and more serious with each passing day. As a result active power filters (APF) gain attention due to their excellent harmonic compensation. But still the performance of the active filter seems to be in contradiction with different control techniques. The main objective of this paper is to analyze shunt active filters employing fuzzy and PI controllers. The active and reactive power method (p-q) is used for the analysis. Extensive simulations were carried out; simulations were performed with balance, unbalanced and non sinusoidal conditions. Simulation results validate the dynamic behaviour of fuzzy logic controller over pi controller.

Keywords— Harmonic compensation, Shunt Active power filters (SHAF), p-q control strategy, PI controller, fuzzy controller

I. INTRODUCTION

Instantaneous active and reactive theory (p-q theory) was introduced in 1984 [1]. Since then, many scientists and engineers [2-5] made significant contributions to its modifications in three-phase four-wire circuits and its applications to power electronic equipment. The p-q theory is based on a set of instantaneous powers defined in the time domain. No restrictions are imposed on the voltage and current waveforms, and it can be applied to three phase systems with or without neutral wire for three phase generic voltage and current waveforms. Thus, it is valid not only in the steady state but also in the transient state. The p-q theory needs an additional Phase locked loop (PLL) circuit for synchronization and therefore p-q method is frequency variant.

Eminent issues always arise in three-phase four-wire systems. It is well-known that zero line may be overheated or cause fire disaster as a result of excessive harmonic current that is going through the zero line (even three times that of normal current). Thus, a perfect compensator is necessary to avoid the consequences due to harmonics. Though several control strategies and controllers have been developed, still the performance of filters is not equivalent under distorted conditions.

Present paper focuses on two controllers (fuzzy and pi) and a filter, employing the instantaneous active and reactive power (p-q) method [6] under different main voltages.

II. SHUNT ACTIVE FILTER CONFIGURATION

To employ APFs in three-phase four-wire systems, two types of configurations are possible; one is a three-leg structure with the neutral conductor being connected to midpoint of dc-link capacitor (Figure 1) and the other one is a four-leg structure, where a fourth leg is provided exclusively for neutral current compensation (Figure 2).

Fig. 1. Three-leg shunt APF with non-linear load.

The four-leg eight-switch APF topology is usually preferred as many researchers have pointed out this configuration as the most proficient alternative to be used in shunt APF [7] (Figure 2). The three-leg six-switch split-capacitor configuration of shunt APF suffers from several shortcomings such as:

(a) Control circuit is somewhat complex
(b) Voltages of the two capacitors of split-capacitor need to be properly balanced
(c) Large dc-link capacitors are required.
However, this topology is sometimes preferred due to less switching devices and lower switching losses compared to the eight-switch topology [8]. The higher order harmonics generated in the eight-switch configuration due to frequent switching of semiconductor devices can be eliminated by the use of RC high-pass filter and switching losses occurring in the VSI can also be minimized by the use of DC-link voltage regulator. Moreover, the four-leg APF has simple dc-link voltage controller, requires small dc-link capacitor, and the control scheme is also quite simple to implement.

![Four-leg shunt APF with non-linear load](image)

III. INSTANTANEOUS ACTIVE AND REACTIVE POWER CONTROL STRATEGY

The control algorithm block diagram for p–q method [1] is shown in Figure 3. The three-phase source voltages \(v_{sa}, v_{sb}, v_{sc}\) and load currents \(i_{La}, i_{Lb}, i_{Lc}\) in the \(a-b-c\) coordinates are algebraically transformed to the \(\alpha-\beta-0\) coordinates using Clarke’s transformation as shown in (1) and (2), followed by the calculation of the instantaneous active power \(p\), reactive power \(q\) and zero-sequence power \(p_0\) as shown in (3).

\[
\begin{bmatrix}
\frac{v_0}{\sqrt{3}} \\
\frac{v_\alpha}{\sqrt{3}} \\
\frac{v_\beta}{\sqrt{3}}
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & 1 & \frac{1}{\sqrt{3}} \\
-\frac{1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{v_a}{\sqrt{3}} \\
\frac{v_b}{\sqrt{3}} \\
\frac{v_c}{\sqrt{3}}
\end{bmatrix}
\]

(1)

\[
\begin{bmatrix}
\frac{i_0}{\sqrt{3}} \\
\frac{i_\alpha}{\sqrt{3}} \\
\frac{i_\beta}{\sqrt{3}}
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \\
\frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{i_{La}}{\sqrt{3}} \\
\frac{i_{Lb}}{\sqrt{3}} \\
\frac{i_{Lc}}{\sqrt{3}}
\end{bmatrix}
\]

(2)

\[
\begin{bmatrix}
\frac{v_0}{\sqrt{3}} \\
\frac{v_\alpha}{\sqrt{3}} \\
\frac{v_\beta}{\sqrt{3}}
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & 1 & 0 \\
\frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{v_a}{\sqrt{3}} \\
\frac{v_b}{\sqrt{3}} \\
\frac{v_c}{\sqrt{3}}
\end{bmatrix}
\]

(3)

\[
p = \frac{v_0}{\sqrt{3}} + \frac{v_\alpha}{\sqrt{3}} + \frac{v_\beta}{\sqrt{3}}
\]

(4)

For reactive and harmonic compensation, the entire reactive power and ac component of active power are utilized as the reference power. The reference currents in \(\alpha-\beta\) coordinates are calculated by using (5).

\[
\begin{bmatrix}
i_{\alpha}^* \\
i_{\beta}^*
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & 1 & 0 \\
\frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{v_0}{\sqrt{3}} \\
\frac{v_\alpha}{\sqrt{3}} \\
\frac{v_\beta}{\sqrt{3}}
\end{bmatrix}
\]

(5)

\[
p = \frac{v_0}{\sqrt{3}} + \Delta p
\]

\[
q = q + \Delta q
\]

The additional average power required to compensate for the losses in VSI due to the switching of semiconductor devices is such that, \(\Delta p = \frac{P_0 + P_{loss}}{2}\), where \(P_{loss}\) is the average value of losses occurring in the inverter and is obtained from the voltage regulator. DC-link voltage regulator is designed to give both good compensation and an excellent transient response. The actual DC-link capacitor voltage \(V_{dc}\) is compared by a reference value \(V_{dc}^*\) and the error is processed in a PI controller.

\[
\begin{bmatrix}
i_{\alpha}^* \\
i_{\beta}^*
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & 1 & 0 \\
\frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{v_0}{\sqrt{3}} \\
\frac{v_\alpha}{\sqrt{3}} \\
\frac{v_\beta}{\sqrt{3}}
\end{bmatrix}
\]

(6)

Appropriate design of PLL allows proper operation under distorted and unbalanced voltage conditions. Controller includes small changes in positive sequence detector as harmonic compensation is mainly concentrated on three phase four wire [9]. In three-phase three wire, \(v'_a, v'_b, v'_c\) are used in transformations given by (7). In three-phase four wire are modified as \(v'_a, v'_b, v'_c\) and given by (8).

\[
\begin{bmatrix}
\frac{v_a}{\sqrt{3}} \\
\frac{v_b}{\sqrt{3}} \\
\frac{v_c}{\sqrt{3}}
\end{bmatrix} = \begin{bmatrix}
\frac{1}{\sqrt{3}} & 1 & 0 \\
\frac{-1}{2} & \frac{1}{2} & \frac{-1}{2} \\
\frac{-1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{3}}
\end{bmatrix} \begin{bmatrix}
\frac{v'_a}{\sqrt{3}} \\
\frac{v'_b}{\sqrt{3}} \\
\frac{v'_c}{\sqrt{3}}
\end{bmatrix}
\]

(7)
Fig. 3. Reference current extraction with conventional p-q method

Fig. 4. Control method for Shunt current compensation based on p-q theory
\[
\begin{align*}
\begin{bmatrix} v_x' \\ v_y' \end{bmatrix} &= \frac{1}{\alpha^2 + \beta^2} \begin{bmatrix} i_x' - i_y' \\ i_y' - i_x' \end{bmatrix} \\
\end{align*}
\]

(8)

IV. CONSTRUCTION OF PI CONTROLLER

Figure 5 shows the internal structure of the control circuit. The control scheme consists of a PI controller, a limiter, and a three phase sine wave generator for reference current generation and generation of switching signals. The peak value of reference currents is estimated by regulating the DC link voltage. The actual capacitor voltage is compared with a set reference value [10].

![Fig. 5. Conventional PI Controller](image)

The error signal is then processed through a PI controller, which contributes to zero steady error in tracking the reference current signal. The output of the PI controller is considered as peak value of the supply current \(I_{\text{max}}\), which is composed of two components: (a) fundamental active power component of load current, and (b) loss component of APF to maintain the average capacitor voltage to a constant value. The peak value of the current \(I_{\text{max}}\) is multiplied by the unit sine vectors in phase with the respective source voltages to obtain the reference compensating currents. This error signal decides the operation of the converter switches. In this current control circuit configuration, the source/supply currents \(I_{abc}\) are made to follow the sinusoidal reference current \(I_{abc}\), within a fixed hysteresis window. The width of hysteresis window determines the source current pattern, its harmonic spectrum and the switching frequency of the devices [11].

The DC link capacitor voltage is kept constant throughout the operating range of the converter. Each phase of the converter is controlled independently. To increase the current of a particular phase, the lower switch of the converter associated with that particular phase is turned on. To decrease the current the upper switch of the respective converter phase is turned on.

V. CONSTRUCTION OF FUZZY CONTROLLER

Figure 6 shows the internal structure of the control circuit. The control scheme consists of a fuzzy controller, a limiter, and a three phase sine wave generator for reference current generation and generation of switching signals. The peak value of reference currents is estimated by regulating the DC link voltage. The actual capacitor voltage is compared with a set reference value. The error signal is then processed through a Fuzzy controller, which contributes to zero steady error in tracking the reference current signal.

![Fig. 6. Conventional Fuzzy Controller](image)

A fuzzy controller converts a linguistic control strategy into an automatic control strategy, and fuzzy rules are constructed by expert experience or knowledge database. Firstly, input voltage \(V_{dc}\) and the input reference voltage \(V_{dc,\text{ref}}\) have been placed of the angular velocity to be the input variables of the fuzzy logic controller. Then the output variable of the fuzzy logic controller is presented by the control current \(I_{\text{max}}\). To convert these numerical variables into linguistic variables, the following seven fuzzy levels or sets are chosen [12]: NB (negative big), NM (negative medium), NS (negative small), ZE (zero), PS (positive small), PM (positive medium), and PB (positive big) as shown in Figure 7.

The fuzzy controller is characterized as follows:

(i) Seven fuzzy sets for each input and output.
(ii) Fuzzification using continuous universe of discourse.
(iii) Implication using Mamdani's 'min' operator.
(iv) Defuzzification using the 'centroid' method.

**Fuzzification:** The process of converting a numerical variable (real number) convert to a linguistic variable (fuzzy number) is called fuzzification.

**Defuzzification:** The rules of FLC generate required output in a linguistic variable (Fuzzy Number), according to real world requirements, linguistic variables have to be transformed to crisp output (Real number).

**Database:** The Database stores the definition of the membership Function required by fuzzifier and defuzzifier.

VI. SIMULATION RESULTS

Figure 8 and Figure 9 illustrates the performance of shunt active power filter under different main voltages. As load is highly inductive, the current is integrated with rich harmonics. Initially, system performance is analyzed with balanced sinusoidal conditions. PI and Fuzzy are good enough in
suppressing harmonics and THD is about 2.85% and 1.27%, but under unbalanced and non-sinusoidal conditions fuzzy shows superior performance over PI controller and THD at this instant with PI are 4.36% and 5.31%, whereas in fuzzy it is about 2.98% and 3.85%. (Figure 10).

VII. CONCLUSION

In the present paper two controllers are developed and verified with three phase four wire system. Even though both controllers are capable to compensate the current harmonics in the 3 phase 4-wire system, it is observed that the fuzzy controller shows more dynamic performance over conventional PI controller. With fuzzy logic and p-q approach a novel shunt active filter can be developed.

<table>
<thead>
<tr>
<th>TABLE I. SYSTEM PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Parameter</strong></td>
</tr>
<tr>
<td>Supply Voltage</td>
</tr>
<tr>
<td>Source Resistance</td>
</tr>
<tr>
<td>Source Inductance</td>
</tr>
<tr>
<td>Filter Phase-branch Resistance</td>
</tr>
<tr>
<td>Filter Phase-branch Inductance</td>
</tr>
<tr>
<td>DC Link Capacitance</td>
</tr>
<tr>
<td>DC Link Voltage</td>
</tr>
<tr>
<td>Hysteresis band</td>
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<tr>
<td>Load</td>
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<tr>
<td>Snubber Resistance</td>
</tr>
<tr>
<td>Snubber Capacitance</td>
</tr>
<tr>
<td>Load Resistance</td>
</tr>
<tr>
<td>Load Inductance</td>
</tr>
</tbody>
</table>

![Fig. 7. Input \( V_{dc} \), Normalized Membership Function.](image)

<table>
<thead>
<tr>
<th>TABLE II. RULE BASE</th>
</tr>
</thead>
<tbody>
<tr>
<td>( V_{dc-ref} )</td>
</tr>
<tr>
<td>NB</td>
</tr>
<tr>
<td>NM</td>
</tr>
<tr>
<td>NS</td>
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<tr>
<td>Z</td>
</tr>
<tr>
<td>PS</td>
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<tr>
<td>PM</td>
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<td>PB</td>
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![Fig. 8. p-q Control Strategy response Under Bal Non-Sin with (a) PI controller (b) Fuzzy controller](image)
Fig. 9. 3ph 4wire Shunt active filter using p-q Control Strategy response Under (a) Bal Sin with PI (b) Bal Sin with Fuzzy (c) Un-bal Sin with PI (d) Un-bal Sin with Fuzzy controller
REFERENCES


AUTHORS PROFILE

Suresh Mikkili was born in Bapatla, Andhra Pradesh, India on 5th Aug 1985. He received B.Tech degree in Electrical and Electronics Engineering from JNTU University Hyderabad in May 2006 and Masters (M.Tech) in Electrical Engineering from N.I.T Rourkela, India in May 2008. He has worked as a Asst.Prof in Electrical Engineering, S.I.T.E, T.P.Gudem from June 2008 to Dec-2009 and in V.K.R & V.N.B Engineering college from Dec-2009 to July 2010. He is currently pursuing the Ph.D degree in Electrical Engineering at N.I.T Rourkela, India from July 2010. His main area of research includes power quality improvement issues, active filters, and soft computing techniques.

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