Nuclear Reactions Fission And Fusion

Describe and give an example of artificial (induced) transmutation

Construct and complete nuclear reaction equations

Artificial transmutation is the changing or manipulation of a nucleus artificially. The nuclear reaction equation below is an example of artificial transmutation:

$${}_{2}^{4}He + {}_{1}^{14}N \rightarrow {}_{8}^{17}O + {}_{1}^{1}H$$

Nitrogen is bombarded with alpha particles (helium) resulting in the creation of oxygen and hydrogen. The alpha particle is absorbed by the nitrogen and a proton (hydrogen w/o an electron) is released. This happened because someone set it up, thus its artificial, and the nitrogen transmutated into oxygen.

Another example of a nuclear reaction is the Fission of Uranium-235 by a slow (thermal) neutron:

$${}^{25}_{02}U + {}^{1}_{0}n \rightarrow {}^{26}_{02}U \rightarrow {}^{90}_{38}Sr + {}^{144}_{54}Xe + 2{}^{1}_{0}n$$

Uranium-235 absorbs a neutron becomes Uranium-236 which is very unstable and quickly breaks down into Strontium and Xeon. This is one of several possible fission reacts, all Uranium fission uses U-235 to create U-236, however the products are not always the same (as with everything quantum-like there are probabilities dictating the outcome).

It is important to note that there are three "conservation laws" that apply to nuclear reactions:

- 1. The number of nucleons in a nuclear reaction is conserved.
- 2. The charge is conserved, or the sum of the charges on the left is equal to the sum of the charges on the right.
- 3. The mass energy is conserved, more on that later...

Define the term unified mass unit

State and apply Einstein's mass-energy equivalence relationship

Explain the concepts of mass defect and binding energy

Solve problems involving mass defect and binding energies

The proton and neutron have very nearly equal mass, albeit very small, approximately. This is not a very convenient number, so a new unit was defined the atomic mass unit, or as the IB likes to call it the unified mass unit, u. One unified mass unit is defined as one-twelfth the mass of a carbon-12 atom. Carbon-12 has 6 protons and 6 neutrons.

This is call an atomic mass unit by Americans, I guess British or the IB likes to be different, who cares. A unified mass unit (u) is defined to be the mass of exactly one—twelfth of a carbon–12 atom. That works out to be:

(2)
$$1 u = 1.66 \times 10^{-27} kg$$

Since the neutron and proton have approximately the same mass, a proton and neutron have approximately mass's of approximately 1 u.

In the IB formula book:

Particle	Mass (u)
Electron (me)	0.000549
Proton (mp)	1.007277
Neutron (mn)	1.008665
Helium Atom	4.002602

If the math is done it can be seen that the helium atom weighs less than the mass of two protons and two neutrons! The same can be found with Oxygen that weighs $15.994915 \, u$, if fact it can be found for all atoms. The difference between the mass of an atom and the sum of an atom's parts is called the mass defect.

The mass defect can be explained by Einstein's mass-energy equivalence:

(3)

 $E=mc^{\Lambda}2$

If you slam to small nuclei into each other and create a bigger atom (but with less mass) then energy is released. The loss of mass is equal to the energy released. For example:

$$_{1}^{1}H+_{1}^{2}H\rightarrow _{2}^{3}He+energy$$

It will take energy to break the new nucleus apart, the energy required to break up a nucleus into in neutron and protons is called the binding energy. In the reaction shown above the energy required to reverse the reaction (break up the helium into hydrogen) is equal to the energy released.

The binding energy of an atom can be approximated summing the mass of the individual neutrons and the mass of the individual protons subtracting the mass of the atom and multiplying by the speed of light squared:

(4)
$$E=[N \cdot mn + Z \cdot mp - massofatom] c^{2}$$

Where N is the number of neutrons, mn the mass of a neutron (u), Z is the number and protons, mp is the mass of a proton (u) and c is the speed of light in MeV u-1.

Describe the processes of nuclear fission and fusion

Things go boom.

The nuclear fission is the process in which a large nucleus splits into two or more smaller nuclei. The only naturally occurring fissionable nucleus is Uranium 235. The Uranium 235 is bombarded with slow or thermal neutrons, the Uranium 235 captures a neutron and becomes Uranium 236 but it is an excited Uranium 236, which is very unstable. The Uranium 236 nucleus quickly decays by fission and splits into two nuclei. If the Uranium 236 atom is allowed to settle to its ground state it will be very stable and has a half of approximately 25 million years. An example of the nuclear equation for the fission of Uranium 235 is shown below:

$$^{25}_{92}U + ^{1}_{0}n \rightarrow ^{236}_{92}U \rightarrow ^{90}_{38}Sr + ^{144}_{54}Xe + 2^{1}_{0}n$$

The products of the nuclear reaction are not always the same. There are several possible by products of the fission of Uranium 235.

Note that in the reaction shown there are 2 neutrons released. If these two neutrons are captured by other Uranium 235 nuclei two more reactions occur and then there are 4 neutrons are released... a chain reaction occurs. This is how nuclear reactor stay on. If the reaction is uncontrolled an explosion occurs.

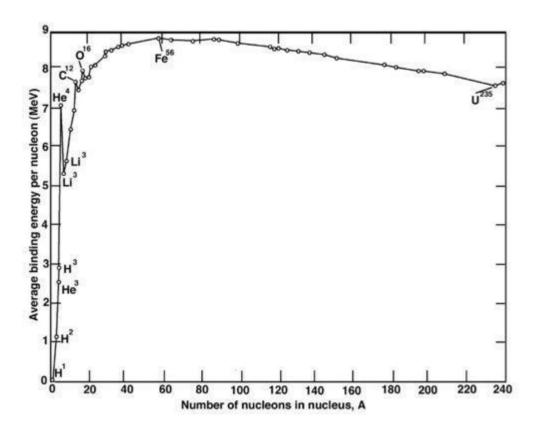
In a nuclear reactor the fuel rods are a mix of Uranium 235 and Uranium 238. The vast majority of the Uranium is Uranium 238 (over 99%) which does not fission. However

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^{238}U with a half-life of 4.5 \times 10^9 years ^{235}U with a half-life of 7 \times 10^8 years ^{234}U with a half-life of 2.5 \times 10^5 years
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Nuclear fusion is simply the joining together of smaller nuclei to create a larger nuclei. The resulting daughter nuclei is less massive than the original mother nuclei. The mass defect is the cause or the source of the energy released in nuclear fusion. An example of nuclear fusion is the fusion of deuterium and tritium: ${}^2D + {}^3T \rightarrow {}^5DHe \rightarrow {}^4He + {}^1n$

In this reaction the deuterium and tritium combine to form He-5 which almost immediately decays to He-4 the emission of a neutron.

So back to binding energy...



To the right is a graph of average binding energy per nucleon vs. atomic number. The greater the binding energy the more stable the nuclei. As a result everything wants to increase its average binding energy per nucleon. Notice that Fe-56 has the highest average binding energy, thus it's the most stable isotope. Everything to the left of Fe-56 tends to fuse (fusion) to create a larger heavier and more stable nuclei. Everything to the right of Fe-56 tends to break down (fission) to become more stable.

This also means that any fission of a nuclei larger than Fe-56 will release energy, whereas isotopes smaller than Fe-56 would require energy to fission... The opposite is true for fusion. Nuclides smaller than Fe-56 will release energy when fused and nuclide larger than Fe-56 will require energy to fuse.